Improved sliding mode observer for FOC control system with discontinuous PWM of sensorless PMSM

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Abstract: With the increasing number of electric cars worldwide, permanent-magnet synchronous motors (PMSMs) are becoming increasingly popular in the transportation industry. In parallel with the development of PMSM, many novel control strategies have been developed to make PMSM superior and robust. In all control strategies aimed at improving the operation of PMSMs, the control strategy using discontinuous pulse width modulation (DPWM) instead of continuous space vector pulse width modulation (CSVPWM) for field-oriented control (FOC) is widely used to reduce switching and save energy. However, this method has not been applied by researchers to sensorless PMSM control three-phase inverters. Therefore, this study investigated a sensorless PMSM control with a DPWM FOC and a traditional sliding-mode observer to estimate rotor positions. Additionally, a modified sliding-mode observer with a Park phase-locked loop (PLL) was designed experimentally to improve the stability of the PMSM speed and reduce harmonics in the output phase current for the inverter under the FOC with DPWM. The experimental results verified that the sliding-mode observer integrated with the Park PLL can improve the operation of the sensorless PMSMs under FOC with DPWM.

Keywords: Sensorless PMSM, Discontinuous Pulse Width Modulation (DPWM), Sliding Mode Observer (SMO), Park Phase-Locked Loop (PLL), Field-Oriented Control (FOC)

1. Introduction

Mechanical engines are gradually being replaced by electrical motors because the earth is gradually exhausted of natural resources and fuel. Electrical motors are utilized not only in electrical vehicles but also in factories, enterprises, and construction sites, and have advantages such as compact size, accurate operation, and environmental friendliness compared to mechanical engines with similar power [1].

Among the types of electric motors, DC motors are more efficient, and the control method is simpler than that of AC motors; however, AC motors require less maintenance and can be easily adapted to various circumstances and environmental conditions. Permanent magnet synchronous motors (PMSMs) are a typical type of AC motors. Compared to other motors, PMSMs are widely used in electric vehicles, aerospace applications, and devices that require high accuracy. PMSMs have several advantages because of their special structure. In a PMSM, the rotor is constructed using a series of permanent magnets, and the stator is wound with a copper wire [2]. PMSMs can achieve a low torque ripple coefficient, high power density, and fast dynamic response by using the magnetic flux generated from the permanent magnets [3][4][5]. To make the PMSMs robust and achieve better power performance, many control strategies have been proposed, such as decreasing power loss by using SIC MOSFETs instead of Si IGBTs [6] or performing an improved MPC [7]. Modifying the PWM scheme in FOC is a simple and effective method. Normally, in FOC, continuous space vector PWM (CSVPWM) is stable and creates fewer harmonics than discontinuous PWM (DPWM). However, DPWM can reduce the switching loss for PMSM control three-phase inverters [8][9][10].

In another development field of PMSM, the mechanical position sensor is removed to reduce the cost and size of PMSM. Therefore, sensorless control strategies for PMSM have become
an interesting topic. Many superior algorithms for estimating the positions of sensorless PMSMs have been proposed. For example, in [11], an improved sliding-mode observer was proposed by integrating adaptive synchronization and a quadrature phase-lock loop. Additionally, a model reference adaptive system (MRAS) [12] was used to estimate the position from the current and voltage of the PMSM in the dq frame. Other complicated computation methods such as the extended Kalman filter (EKF) [13][14] and Luenburger observer were used [15].

However, the research papers only focus on developing position estimation algorithms for sensorless PMSM and conducting experiments with a continuous space vector PWM based on FOC. Thus, this paper presents a method for estimating the angular position of a motor using a sliding mode observer (SMO) modified to improve efficiency and reduce harmonics for the motor current with a DPWM strategy based on FOC.

2. Mathematical Model of PMSM

Determining a PMSM model is important for precisely and effectively controlling PMSM. The equation of state for PMSMs in the dq frame can be expressed as follows:

\[
\begin{align*}
\frac{d}{dt}i_d &= \frac{1}{L_s}(-R_s i_d + \omega_r L_s i_q + u_d) \\
\frac{d}{dt}i_q &= \frac{1}{L_s}(-R_s i_q + \omega_r L_s i_d - \omega_r \psi_f + u_q)
\end{align*}
\]

(1)

where \(i_d\) and \(i_q\) are the dq axis stator currents, and \(u_d\) and \(u_q\) are the dq axis stator voltages. \(\omega_r\) is the rotor electrical speed, and \(\psi_f\) is flux linkage. \(R_s\) and \(L_s\) are the resistance and inductance of the stator, respectively.

And in \(\alpha\beta\) stationary reference frame as:

\[
\begin{align*}
\frac{d}{dt}i_\alpha &= \frac{1}{L_s}(-R_s i_\alpha - e_\alpha + u_\alpha) \\
\frac{d}{dt}i_\beta &= \frac{1}{L_s}(-R_s i_\beta - e_\beta + u_\beta)
\end{align*}
\]

(2)

Here \(i_\alpha\) and \(i_\beta\) and \(u_\alpha\) and \(u_\beta\) are \(\alpha\beta\) stationary reference frame currents and voltages, respectively. Additionally, \(e_\alpha\) and \(e_\beta\) are \(\alpha\beta\) frame back electromotive forces (back emf), which are described as

\[
\begin{align*}
e_\alpha &= -\psi_f \omega_s \sin \theta \\
e_\beta &= \psi_f \omega_s \cos \theta
\end{align*}
\]

(3)

Using Equation (3), the position and speed of PMSM rotors can be calculated as follows:

\[
\begin{align*}
\theta &= -\arctan \frac{e_\alpha}{e_\beta} \\
\omega_r &= \frac{\sqrt{e_\alpha^2 + e_\beta^2}}{\psi_f}
\end{align*}
\]

(4)

Based on the above equations, the observer and control strategies for PMSMs are discussed and established in the subsequent sections.

3. Field-Oriented Control Strategy for PMSM

3.1 Conventional Field-Oriented Control

Field-oriented control (FOC) is a well-known method for three-phase motor control. In the three-phase PMSM control with a position sensor, as shown in Figure 1, the position signal of the rotor is used to calculate the speed of the motor and then provide feedback for comparison with the reference speed.

Figure 1: Field-oriented control block diagram with a sensor PMSM

Normally, the SVPWM block in the FOC operates with continuous space-vector pulse-width modulation (CSVPWM). CSVPWM is shown in Figure 2. CSVPWM has a power loss problem owing to its high switching loss. Hence, discontinuous pulse-width modulation (DPWM) was used instead of CSVPWM. Although DPWM produces more harmonics in the
output current than CSVPWM, DPWM can significantly reduce the switching loss of a three-phase inverter. Switching loss is the amount of power loss in semiconductor switches when the inverter operates at a high frequency. This phenomenon cannot be avoided by reducing the size of the device or by reducing harmonics. Therefore, the device must operate under high-frequency conditions.

3.2 Discontinuous Pulse-Width Modulation for Field-Oriented Control System

Fundamentally, the DPWM operation for the three-phase inverter control of PMSMs is the creation of either one of two ineffective voltage vectors, namely, the zero vector or the seventh ineffective voltage vector within a single switching cycle. This is in contrast to CSVPWM, which generates both ineffective voltage vectors during each switching cycle. With this strategy, the control system can reduce the ineffective voltage vectors and the number of switchings. The two typical variants of DPWM in the PMSM-controlled three-phase inverter introduced in this study are DPWMMIN and DPWMMAX. Graphical representations of the DPWMMIN and DPWMMAX waveforms are shown in Figure 3.

4. Design of Sliding Mode Observer for Sensorless PMSM Controlled with DPWM

4.1 Conventional Sliding Mode Observer

A conventional sliding mode observer (SMO) was established using the \( \alpha\beta \) stationary reference frame voltage equation to observe rotor position and estimate the speed of sensorless PMSM based on back electromotive force (back emf). Figure 4 shows a conventional sliding mode observer diagram with the rotor position and speed in the output.

![Figure 4: Conventional sliding mode observer diagram](image)

In the sliding mode observer, back emf was obtained from the difference between the estimated \( \alpha\beta \) currents and real measured currents of the motor with signum function and low pass filter. The real measured currents are \( i_\alpha \) and \( i_\beta \) and the real measured voltages are \( v_\alpha \) and \( v_\beta \). The estimated \( \alpha\beta \) currents were calculated using Equation (5).

\[
\begin{align*}
\frac{di_\alpha}{dt} &= -\frac{1}{L_s}(R_s i_\alpha - v_\alpha + K \text{sign}(i_\alpha - i_\alpha)) \\
\frac{di_\beta}{dt} &= -\frac{1}{L_s}(R_s i_\beta - v_\beta + K \text{sign}(i_\beta - i_\beta))
\end{align*}
\]

(5)

where K is the gain of the observer and is multiplied by the sign function. K gain must be sufficiently large and satisfy the condition of \( K > \max(|e_\alpha||e_\beta|) \). And back emf is as Equation (6).
\[ z_a = K \text{sign}(i_a - i_a) \]
\[ z_b = K \text{sign}(i_b - i_b) \]

Because \( z_a \) and \( z_b \) include a large number of interferences to achieve accurate back emf (\( e_a \) and \( e_b \)), using low pass filter (LPF) for the value of \( z_a \) and \( z_b \) is necessary.

\[
\begin{aligned}
\hat{\theta}_a &= \frac{w_c}{\tau + w_c} z_a \\
\hat{\theta}_b &= \frac{w_c}{\tau + w_c} z_b
\end{aligned}
\]

where \( w_c \) is the cut-off frequency and \( \tau \) is the time constant of LPF. Thus, based on Equation (4), the position and speed of the rotor can be estimated using Equations (8) and (9).

\[
\hat{\theta} = - \arctan \left( \frac{\hat{e}_b}{\hat{e}_a} \right)
\]

\[
\hat{\omega}_e = \frac{d}{dt} \hat{\theta}
\]

Using a conventional sliding-mode observer, an experiment was conducted to evaluate the observer’s ability, and the results are presented in the experimental section.

4.2 Integrating Sliding Mode Observer with Park Phase-Locked Loop

![Figure 5: Improved sliding mode observer with a Park phase-locked loop block diagram](image)

Conventional sliding-mode observers have some weaknesses in that they cannot completely attenuate the interference and chatter in the estimated position signal. Because of the disturbance that appears in the estimated position signal, the output current can also be affected and distorted. Therefore, this study proposed an improved sliding-mode observer with a Park-phase-locked loop. In the proposed method, the estimated \( \alpha\beta \) frame back emf is exchanged to the \( dq \) frame. By exchanging the \( dq \) frame, the \( dq \) frame back EMF signal had two direct lines; therefore, it was more effective when implementing two filters in the output. Hence, the output signal was attenuated by interference and chattering. A block diagram of the sliding-mode observer with a Park phase-locked loop is shown in Figure 5.

As illustrated in the block diagram, the Park block converted the \( \alpha\beta \) frame back emf to \( dq \) frame back emf. The conversion was implemented using Equation (10).

\[
\begin{bmatrix}
\hat{e}_d \\
\hat{e}_f
\end{bmatrix} = \frac{w_{c2}}{\tau + w_{c2}} \begin{bmatrix}
\hat{e}_d \\
\hat{e}_f
\end{bmatrix}
\]

After the conversion process, the values of the returned emf and \( dq \) components were filtered through a first-order filter. Here, the first-order filter was a low-pass filter.

\[
\begin{bmatrix}
\hat{e}_d \\
\hat{e}_f
\end{bmatrix} = \frac{w_{c2}}{\tau + w_{c2}} \begin{bmatrix}
\hat{e}_d \\
\hat{e}_f
\end{bmatrix}
\]

where \( w_{c2} \) is cut-off frequency and different from the cutoff frequency in Equation (7). The rotor position was obtained using Equation (12).

\[
\hat{\theta} = \int \frac{1}{K_g} (\hat{e}_{df} - \text{sign}(\hat{e}_{df}) \cdot \hat{e}_{df})
\]

In the above equation, \( K_g \) is the voltage gain, and the sign is the signum function. The speed was obtained easily by deriving the estimated rotor position.

\[
\hat{\omega}_e = \frac{d}{dt} \hat{\theta}
\]

With an additional Park PLL at the output of the SMO, the interference and chattering of the estimated rotor-position signal were significantly reduced. Hence, the output current in the inverter phases were more stable and the harmonics were reduced. The results of this method are compared with those of the conventional SMO in the experimental results section.

5. Experiment and Results

5.1 Experiment Configuration

Figure 6 shows a block diagram of the Sensorless PMSM control method. The control method was field-oriented with a modified sliding-mode observer to respond to speed and position feedback. The DPWMMAX strategy was utilized in the SVPWM block, and the parameters of the PMSM used to compute the SMO are listed in Table 1.
Table 1: Parameters of PMSM used in the experiment

<table>
<thead>
<tr>
<th>Quantity</th>
<th>Symbol</th>
<th>Nominal value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Stator resistance</td>
<td>$R_s$</td>
<td>1.1 Ω</td>
</tr>
<tr>
<td>Stator inductance</td>
<td>$L_s$</td>
<td>0.07803 mH</td>
</tr>
<tr>
<td>Number of rotor</td>
<td>$P$</td>
<td>4</td>
</tr>
<tr>
<td>DC-link voltage</td>
<td>$V_{dc}$</td>
<td>24 V</td>
</tr>
<tr>
<td>Moment of intertia</td>
<td>$J$</td>
<td>0.004 $kg - m^2$</td>
</tr>
<tr>
<td>Rated speed</td>
<td>$T_R$</td>
<td>0.062 N·m</td>
</tr>
<tr>
<td>Reted torque</td>
<td>$N_R$</td>
<td>4000 r/min</td>
</tr>
<tr>
<td>Reference speed</td>
<td>$\omega_{ref}$</td>
<td>700 rpm</td>
</tr>
</tbody>
</table>

The experimental setup for the sensorless PMSM is shown in Figure 7. The system used a three-phase variable DC power supply to provide a 24 V DC input to the inverter. The 24 V DC input was converted to a three-phase AC voltage for application to the PMSM. In the DC-to-AC converter board, six IGBTs were controlled in the gate terminal by a switching pulse. Switching pulses were generated using a DSP TMS320F28335D on the control board. The DSP TMS320F28335D also implemented the proposed algorithm and received an analog feedback signal from the sensors on the control board. The experimental data were saved and plotted in MATLAB using a JTAG emulator (XDS 300S) of Syncworks, and the current waveform and switching pulse were measured using a digital oscilloscope.

5.2 Results of the Experiment

A. Conventional Sliding Mode Observer

Figure 8 shows the rotor position estimated using a conventional sliding-mode observer and the actual rotor position measured using a mechanical encoder integrated with the PMSM. Using Figure 8 as a reference, it can be observed that the estimated rotor position closely approximated the rotor position determined by the encoder. However, the estimated signal exhibited discernible chatter and lacked clarity. Owing to the presence of noise in the estimated rotor position, the operational performance of the IGBT gate drivers, specifically the speed and reference switching times, was adversely affected.

As shown in Figure 9, the motor speed was unstable between 600 and 700 rpm, and the reference phase-voltage waveform became distorted compared with the ideal phase-voltage waveform shown in Figure 3(a). In addition, the inverter operated with the gate-drive switching pulses of the DPWMMAX, and the output phase current is shown in Figure 10.

Under the feedback signals of the conventional SMO, the total harmonic distortion of the output phase current was 40.92% at a fundamental frequency of 60 Hz, as shown in Figure 11.
Figure 10: IGBT gate drive pulse and output phase current

Figure 11: Output phase current total harmonic distortion

B. Improved Sliding Mode Observer with Park PLL

Figure 12: Estimated and actual rotor positions.

Figure 13: Reference phase voltage of DPWM and motor’s speed

Similar to the conventional sliding-mode observer, Figure 12 shows the estimated rotor position obtained using the sliding-mode observer in conjunction with a Park PLL. This estimated position was closer to the actual rotor position, and the chatter was significantly reduced. Therefore, the speed of the motor was more stable at 700 rpm. The reference phase voltage waveform is as ideal phase voltage waveform in Figure 3(a) as shown in Figure 13, and the phase current waveform was almost sinusoidal, as shown in Figure 14.

Figure 14: IGBT gate drive pulse and output phase current

Figure 15: Output phase current total harmonic distortion

Additionally, the harmonics existing in the current phase were significantly reduced, as indicated by the THD coefficient shown in Figure 15.

In the case of a PMSM operating with an improved sliding-mode observer with a Park PLL, the total harmonic distortion of the output phase current was 25.40% at a fundamental frequency of 60 Hz, as shown in Figure 15.

6. Conclusion

This study proposed an improved sliding mode observer with the Park phase-locked loop algorithm for estimating the rotor position of PMSMs under DPWM FOC.

Under similar conditions and input references between a conventional SMO and the improved sliding mode observer with the Park phase-locked loop, by the improved sliding mode observer the results were obtained:

1. the position of the rotor was accurately estimated without chatters or interferences;
2. the output speed of the PMSM was more stable when the reference speed was 700 rpm;
3. the experimental results show that the harmonics in the
current of phases decreased significantly from 40.92% to 25.40% compared to those using a conventional SMO.

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**Author Contributions**

Conceptualization, V. V. HUNG, K. K. Yoon and S. G. Lee; Methodology, V. V. HUNG, K. K. Yoon and S. G. Lee; Software, V. V. HUNG; Formal Analysis, V. V. HUNG and S. G; Investigation, V. V. HUNG and K. K. Yoon; Data curation V. V. HUNG and S. G Lee; Writing Original Draft Preparation, V. V. HUNG; Writing-Review & Editing, S. G. Lee; Visualization, V. V. HUNG and K. K. Yoon; Supervision, S. G. Lee; Project Administration, K. K. Yoon and S. G. Lee; Funding Acquisition, S. G. Lee.

**References**


